

情報可視化における 最適化モデルの定式化

会津大学
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可視化(ビジュアライゼーション)

- 複雑な対象データの特徴をコンピュータグラフィックス技術を用いて効果的に視覚化する技術
- 「百聞は一見にしかず」

可視化の要素技術

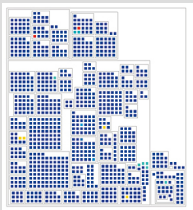
- Scientific Visualization
科学的可視化
 - 数値データの可視化技法(空間構造あり)
- Information Visualization
情報可視化
 - 抽象データの可視化技法(空間構造なし)
- Visual Analytics
視覚分析論
 - 可視化と対話処理の融合による知識発見

多変量データの可視化

Scatterplot matrix

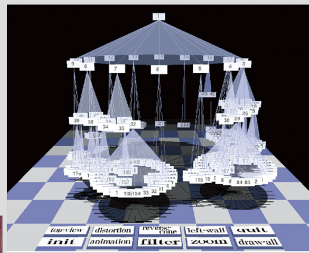
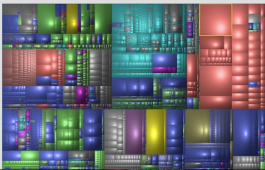
Parallel coordinates

ツリーの可視化



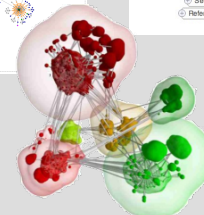
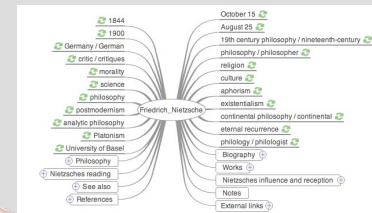
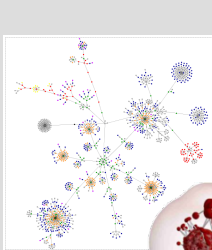
平安京ビュー

Treemap

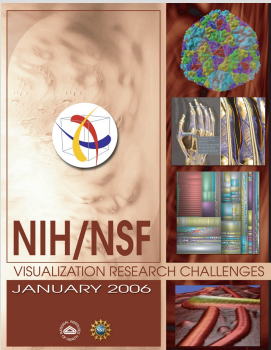


Cone tree

グラフの可視化



VRC Report

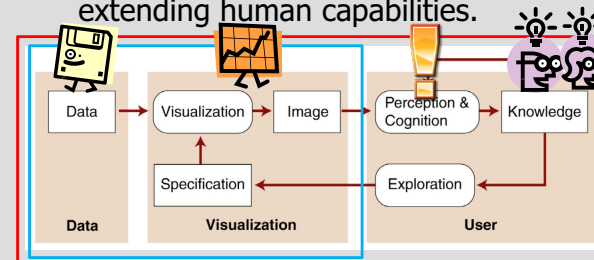


- ViSCLレポート(1987)の後継版
- IEEE Vis. 2005 でドラフト配布
- 2006.1 最終版
<http://tab.computer.org/vgtc/vrc/>

7

Visualization Discovery Process

- Visualization systems are explicitly designed not to replace the human but to keep the **human in the loop** by extending human capabilities.





情報可視化の技術的課題

- 最適化問題として定式化
 - データのクラスタリングや分類
 - 視覚表現の図式化およびレイアウト問題
- 個々の解のモデル化は問題ごとに異なる
- 共通の最適化手法が広範囲の問題に適用可能

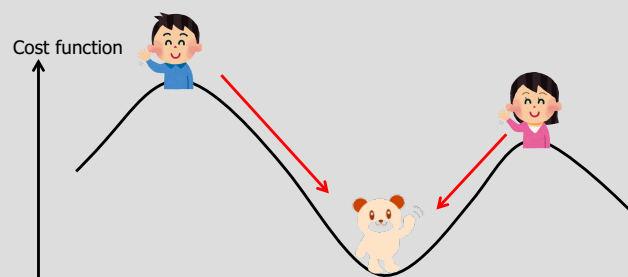


Overview

Gradient methods

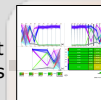


Gradient Method

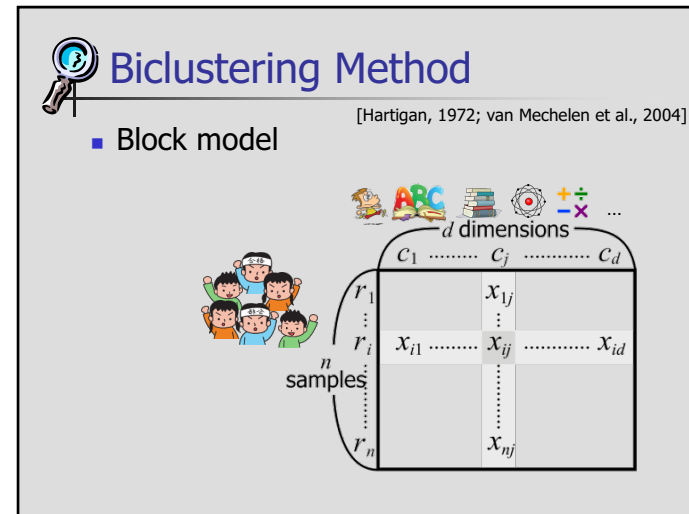
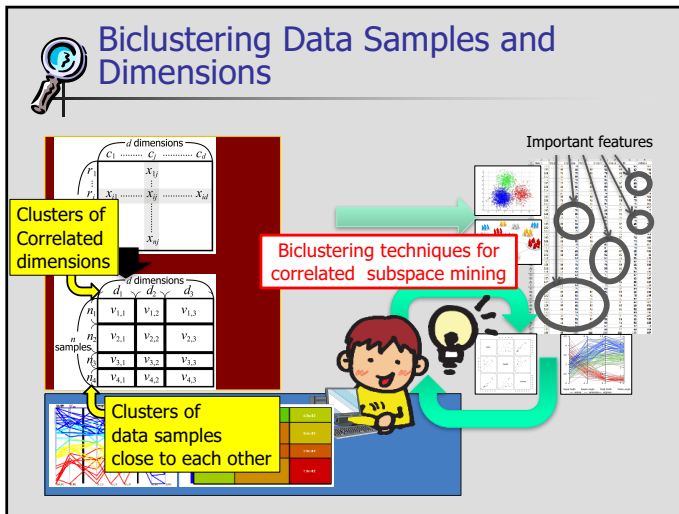
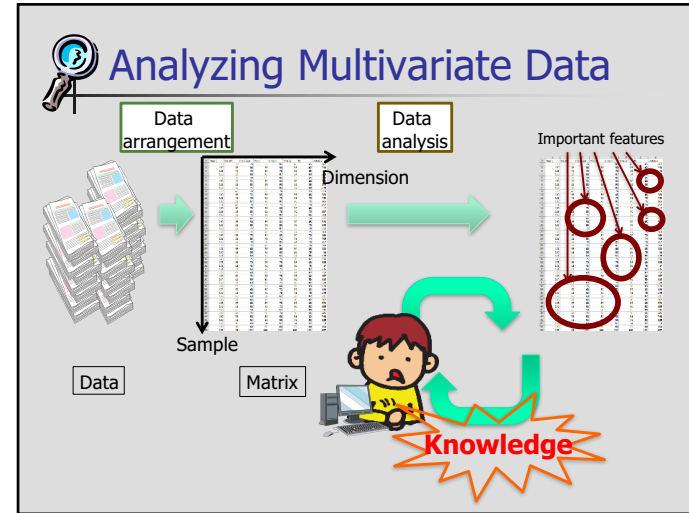
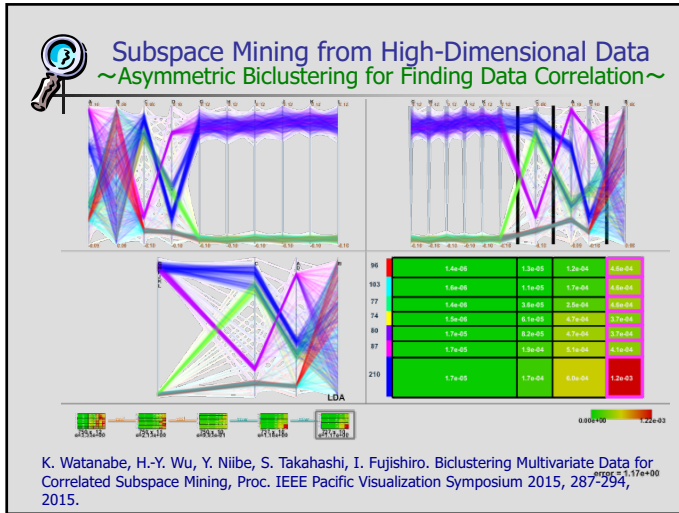


Overview

Gradient methods



Multivariate analysis



K-means Clustering

- Minimize the sum of distances from the corresponding cluster centers

height, BMI, PE class, distance, literature, English, math, physics, ...

$$\min \sum_{i=1}^n \|r_i - \theta_{\kappa(i)}\|^2$$

Biclustering Method

[Hartigan, 1972; van Mechelen et al., 2004]

- Block model
 - Symmetric application of K-means to rows and columns

K-means OK??

K-means OK!!

$$\min \sum_{i=1}^n \sum_{j=1}^d (x_{ij} - v_{\kappa(i), \lambda(j)})^2$$

$v_{1,1}$	$v_{1,2}$	$v_{1,3}$
$v_{2,1}$	$v_{2,2}$	$v_{2,3}$
$v_{3,1}$	$v_{3,2}$	$v_{3,3}$
$v_{4,1}$	$v_{4,2}$	$v_{4,3}$

Normalization

- Projected onto a high-dimensional sphere

\mathbb{R}^n

S^{n-1}

n students

$$\max \sum_{j=1}^d \tilde{c}_j \cdot \mu_{\lambda(j)}$$

Spherical K-means Clustering

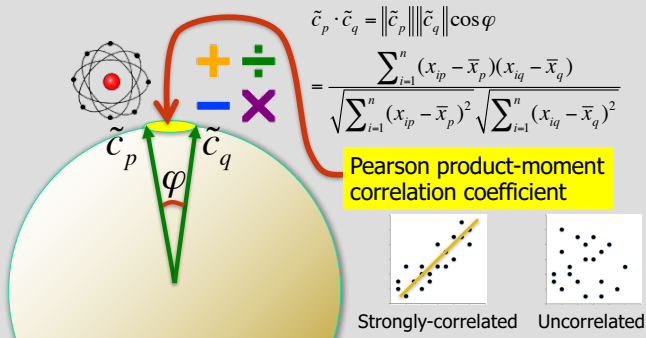
- Inner product represents correlation

Inner product

$$\max \sum_{j=1}^d \tilde{c}_j \cdot \mu_{\lambda(j)}$$

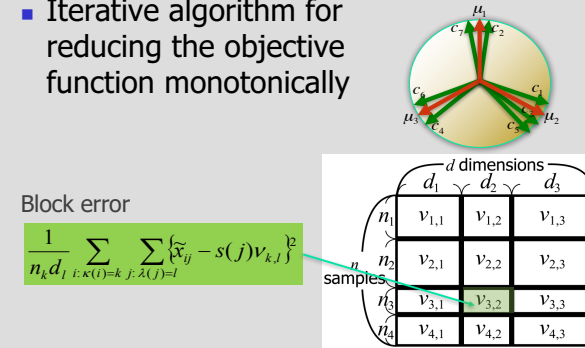
Spherical K-means Clustering

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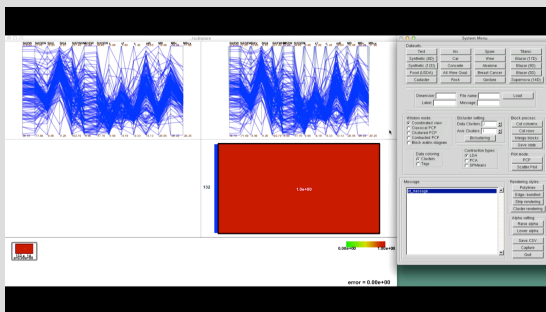


Asymmetric Biclustering

- Iterative algorithm for reducing the objective function monotonically

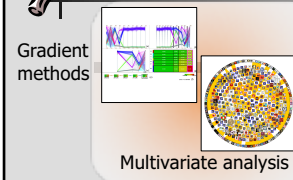


Type Ia Supernova Data



Data is provided by courtesy of Professor Uemura of Hiroshima Univ.

Overview



Anchored Maps of Image Feature Space

~Projecting High-Dimension through Bipartite Relationships~

Feature space

Images Representative features

The bipartite graph

Anchored Map Representation

Representative features

Coarse level Fine level

Y. Gao, H.-Y. Wu, K. Misue, K. Mizuno, S. Takahashi. Visualizing Bag-of-Feature Image Categorization Using Anchored Maps. Proc. VINCI 2014, 39-48, 2014.

Bag-of-Features Model

- Associate each image with a set of features

Representative features

Feature space

Images Representative features

The bipartite graph

Visualizing Bipartite Relationships

- Visualize the bipartite graph using anchored map representations

Images Representative features

Bipartite graph

Landmarks

Anchored map

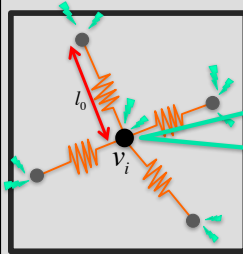
Anchored Map Representation

- Force-directed algorithm is employed



The Force Directed Algorithm

- Avoid excessive visual clutter using drawing and repulsive forces



l_0 : original length

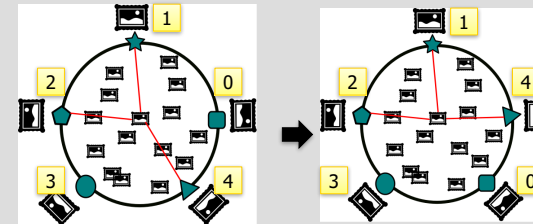
$$F_s(v_i) = \sum_{j \in N_i} k_d (|v_i - v_j| - l_0)(v_j - v_i) - \sum_{k \in V - \{i\}} \frac{k_r (v_k - v_i)}{|v_i - v_k|^2}$$

Drawing force
Repulsive force



Anchored Map Representation

- Genetic-based optimization
 - improve the visual readability of the anchored map.

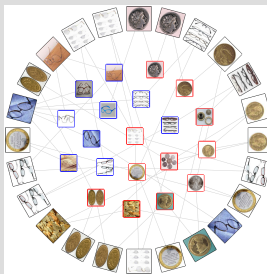


Gene [0 1 2 3 4]

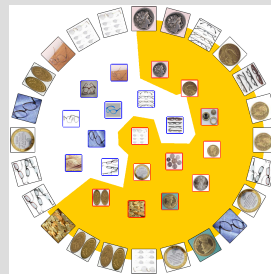
[4 1 2 3 0]



Anchored Map Representation



Original layout



With an optimized circular ordering of features



Demonstration

- Discriminate car images from others.

System Demo

Cars, tomatoes, and grapes

Overview

Gradient methods

Multivariate analysis

Linear programming

Linear Programming (LP)

- Inequality constraints

$$3x - 4y \geq 4$$

$$x \leq 6$$

$$9x + 25y \geq 50$$
- Objective function

$$\text{minimize } c = x + 2y$$

Linear Programming (LP)

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Linear Programming (LP)

Inequality constraints

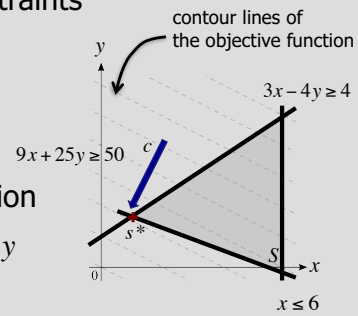
$$3x - 4y \geq 4$$

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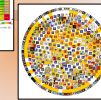


Overview

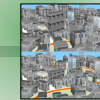
Gradient methods



Multivariate analysis



Map composition

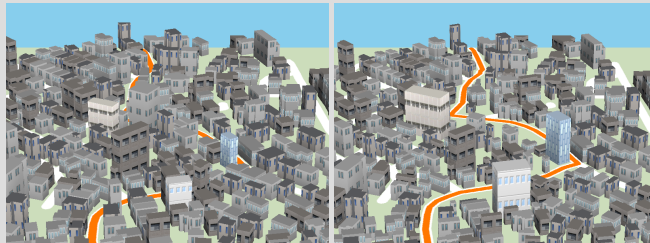
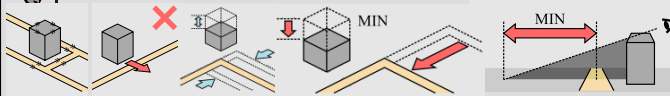


Linear programming



Disoccluding Routes in Urban Maps

~Constrained Optimization for 3D Urban Map Layouts~



D. Hirono, H.-Y. Wu, M. Arikawa, S. Takahashi. Constrained Optimization for Disoccluding Geographical Landmarks in 3D Urban Maps, Proc. IEEE Pacific Visualization Symposium 2013, 17-14, 2013.



Hand-Drawn Urban Maps

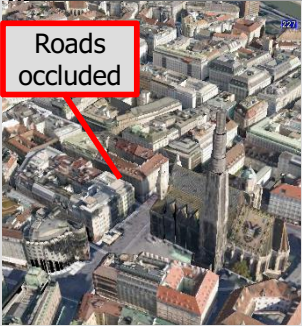


Synthesized map
(by Google earth)




Hand-drawn map
(by ATP Jihlava)

Hand-Drawn Urban Maps



Roads occluded

Synthesized map
(by Google earth)

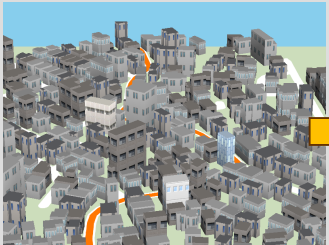



Roads visible

Hand-drawn map
(by ATP Jihlava)

Goal

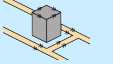
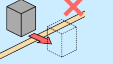
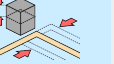

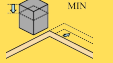
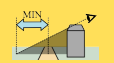
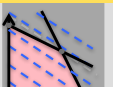
Deform 3D urban maps to enhance their readability

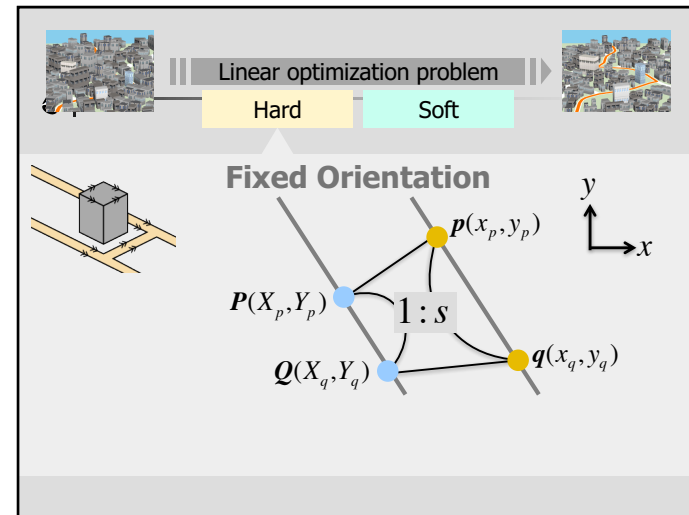
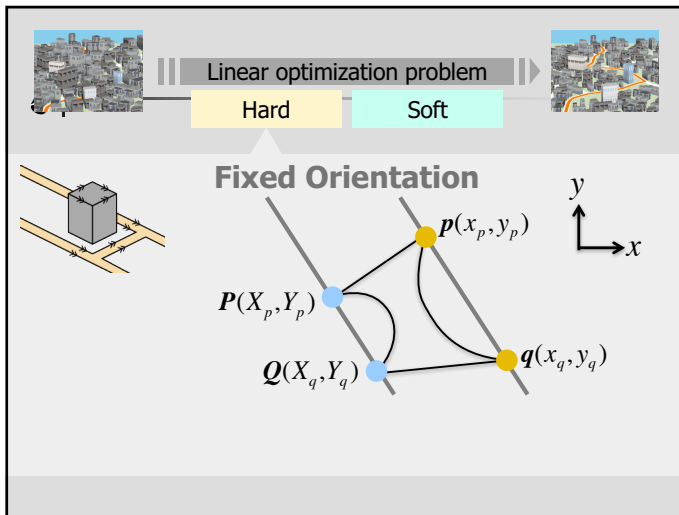
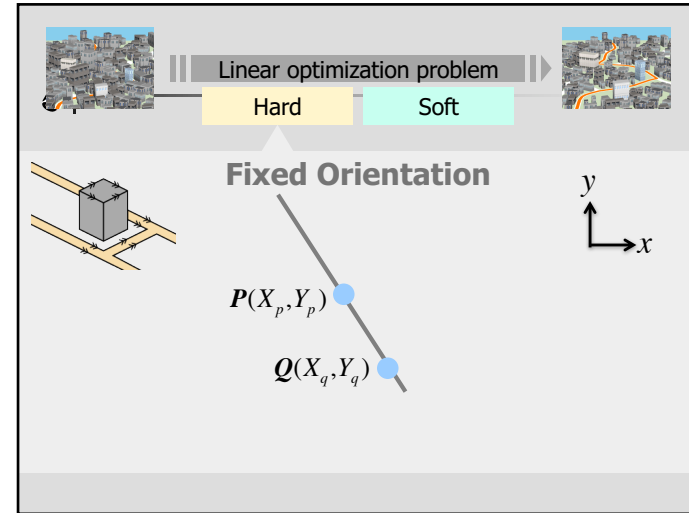
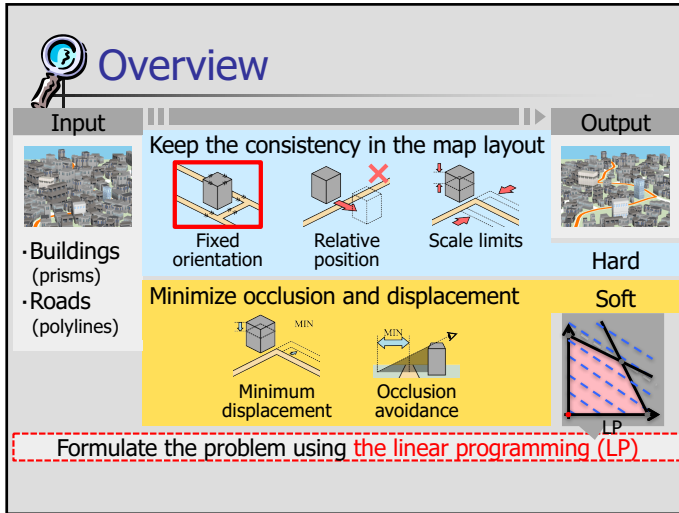



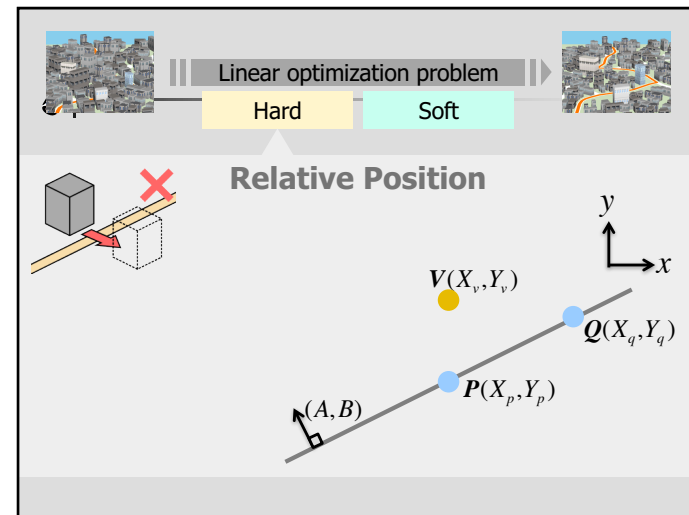
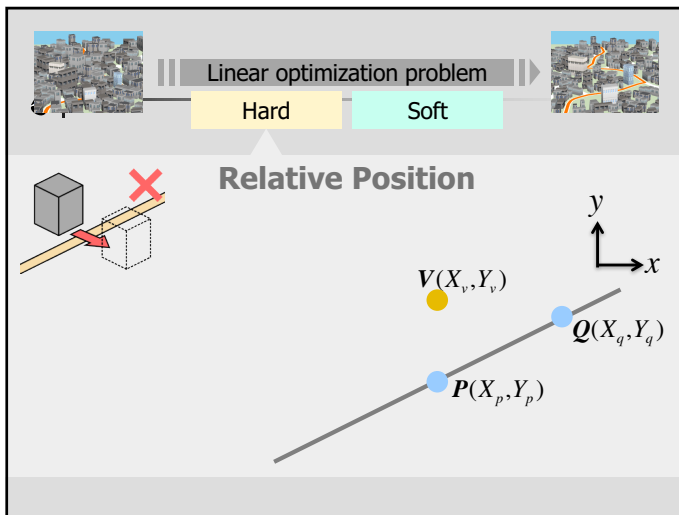
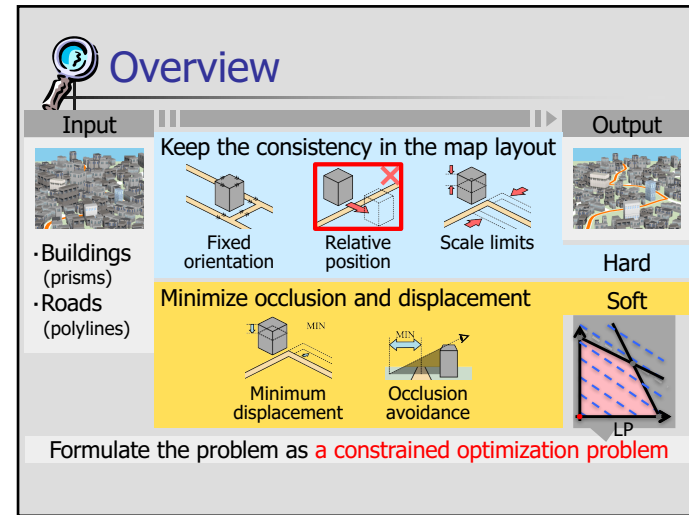
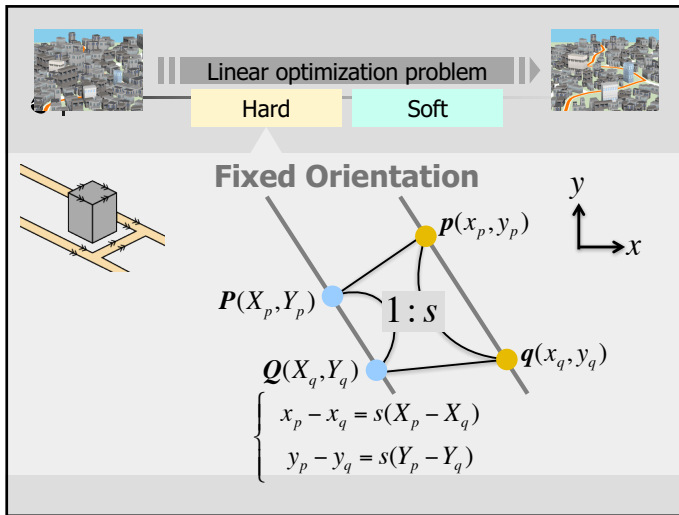
Original layout Optimized layout

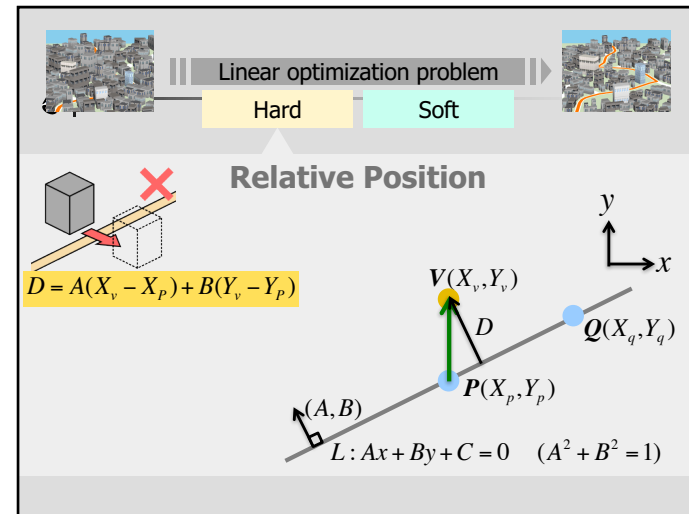
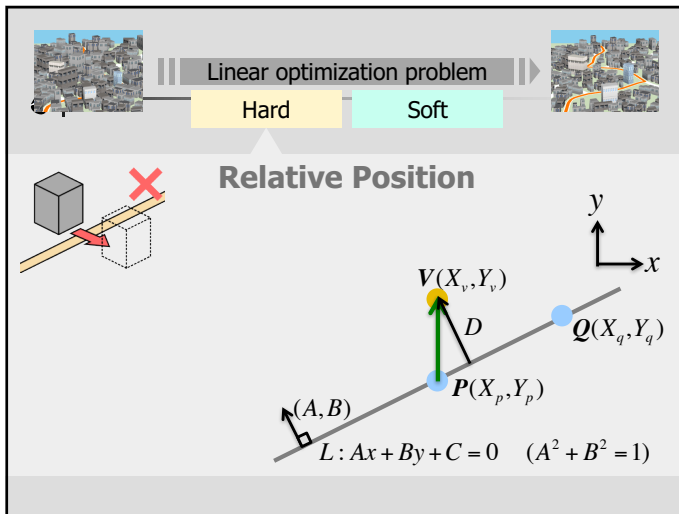
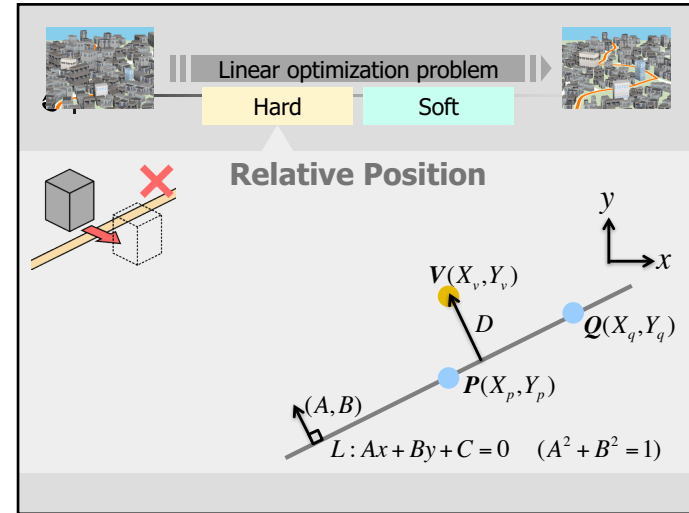
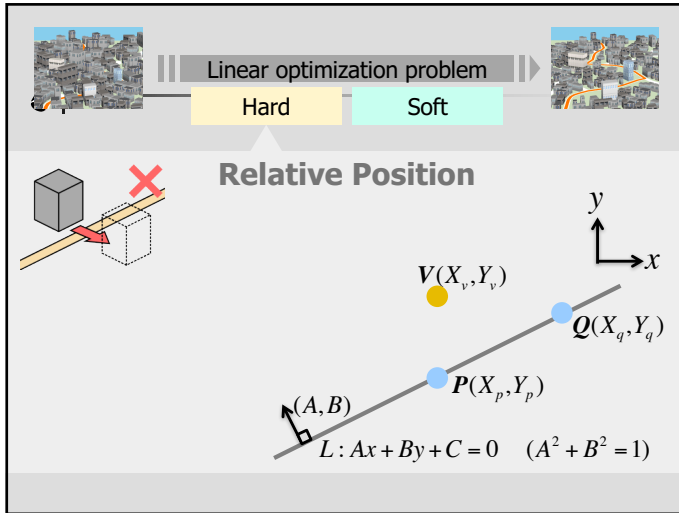


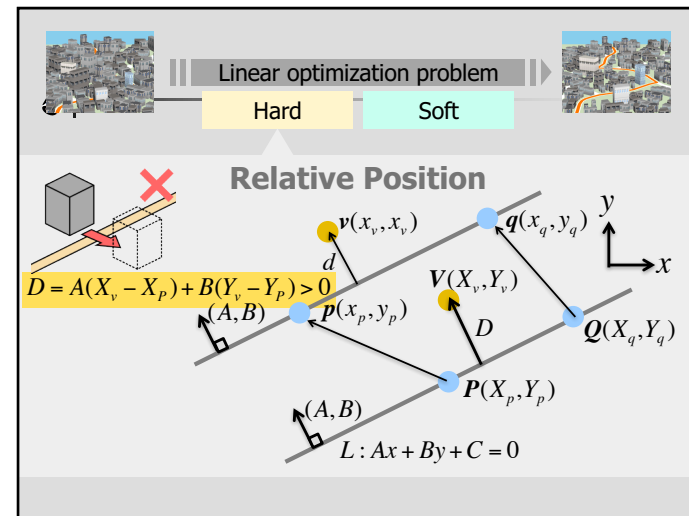
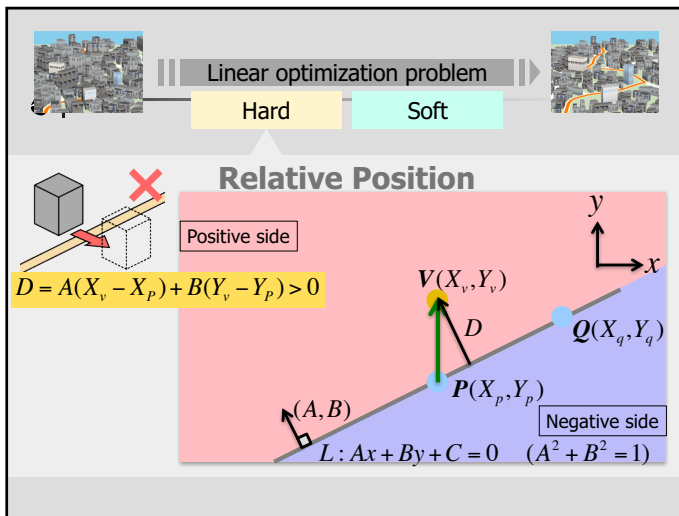
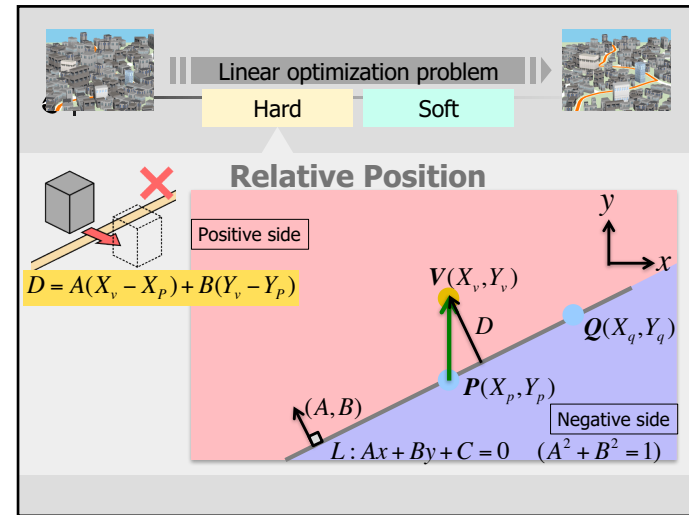
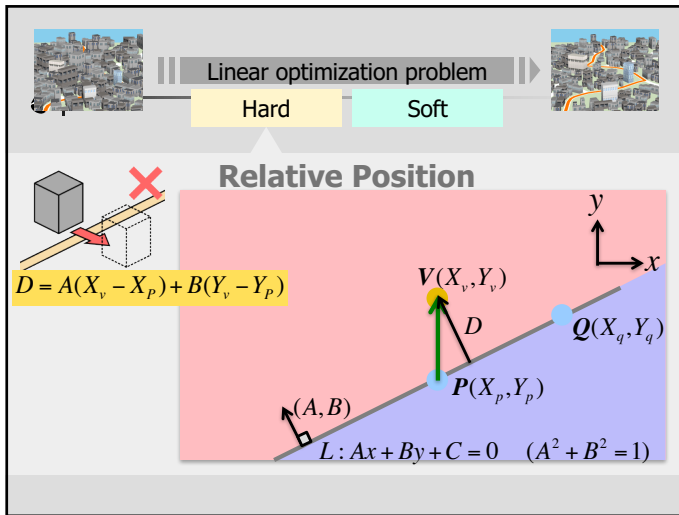
Overview

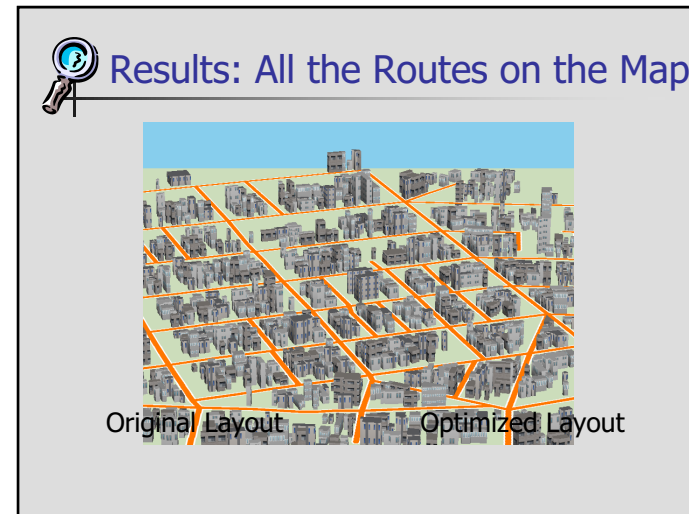
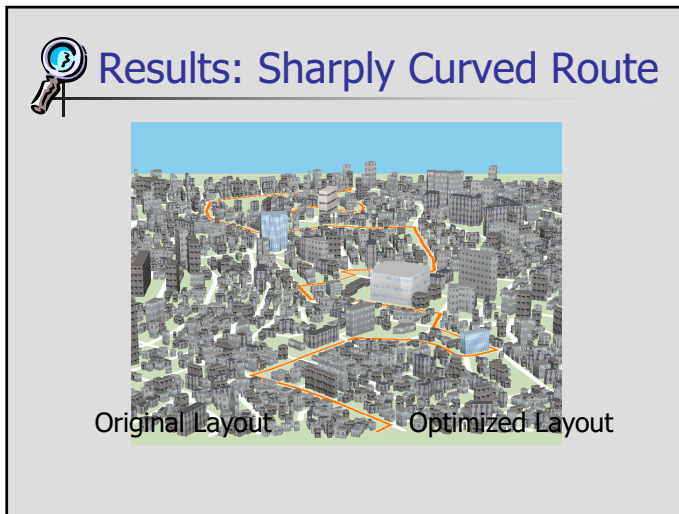
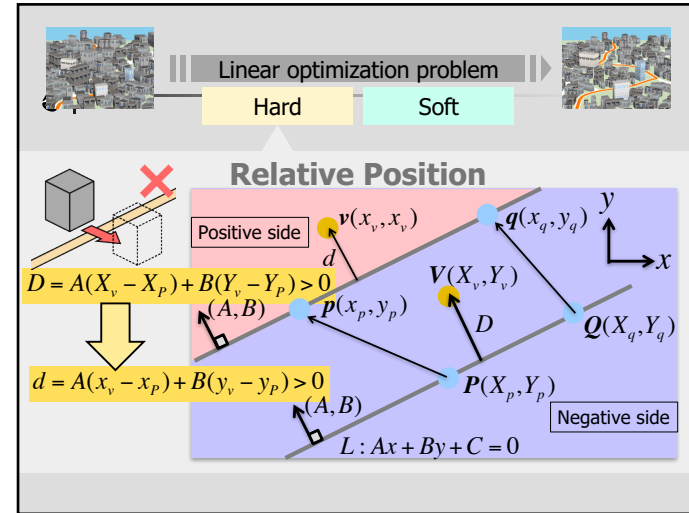
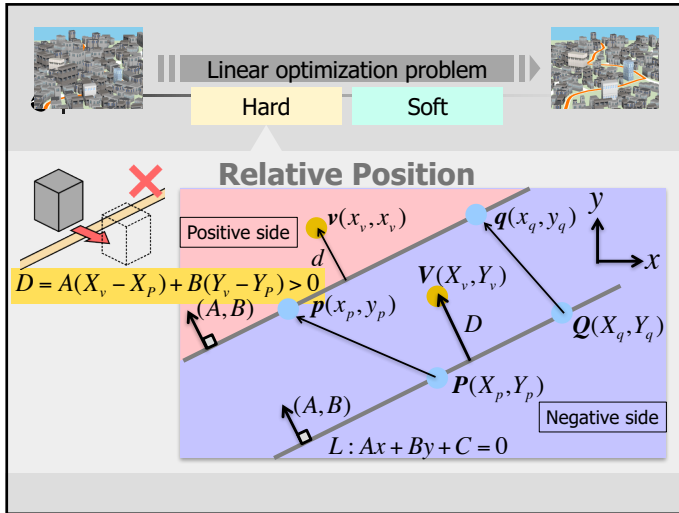
Input	Keep the consistency in the map layout	Output
<ul style="list-style-type: none"> • Buildings (prisms) • Roads (polylines) 	<div style="display: flex; justify-content: space-around;"> <div style="text-align: center;">  Fixed orientation </div> <div style="text-align: center;">  Relative position </div> <div style="text-align: center;">  Scale limits </div> </div>	 Hard
	<div style="background-color: yellow; padding: 5px;"> <p style="text-align: center; margin: 0;">Minimize occlusion and displacement</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;">  Minimum displacement </div> <div style="text-align: center;">  Occlusion avoidance </div> </div> </div>	<div style="background-color: yellow; padding: 5px;">  Soft </div>
Formulate the problem using the linear programming (LP)		





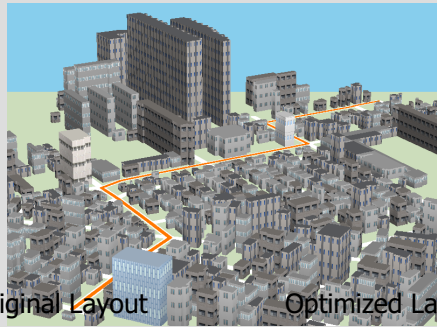








Results: Landmark Buildings

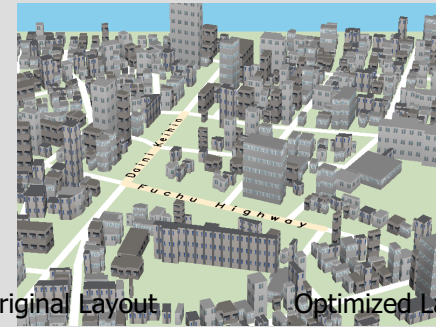


Original Layout

Optimized Layout



Results: Annotating Roads




Original Layout

Optimized Layout



Results: Statistics

					
Preprocess	1.2 sec	15.6 sec	6.7 sec	2.4 sec	2.7 sec
Optimization	3.1 sec	53.0 sec	12.7 sec	6.9 sec	8.4 sec
Number of variables	12,372	117,724	45,774	22,363	25,490
Number of constraints	34,057	322,615	105,690	59,067	66,550
Elevation angle	25	20	20	20	30



Overview

Gradient methods



Multivariate analysis



Map composition

Linear programming



Integer programming

Linear Programming (LP)

- Inequality constraints

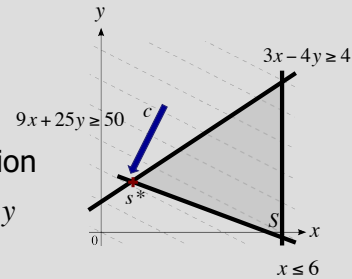
$$3x - 4y \geq 4$$

$$x \leq 6$$

$$9x + 25y \geq 50$$

- Objective function

$$\text{minimize } c = x + 2y$$



Mixed-Integer Programming (MIP)

- Inequality constraints

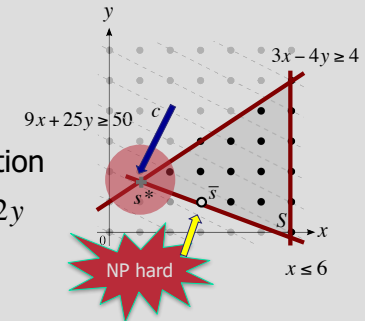
$$3x - 4y \geq 4$$

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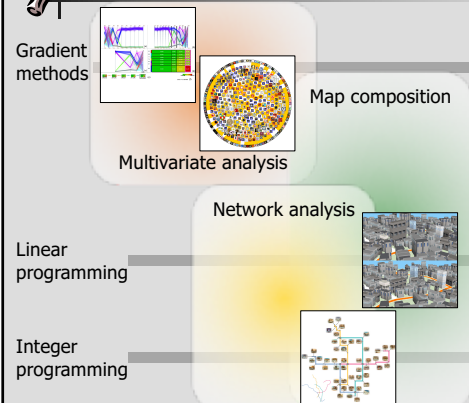
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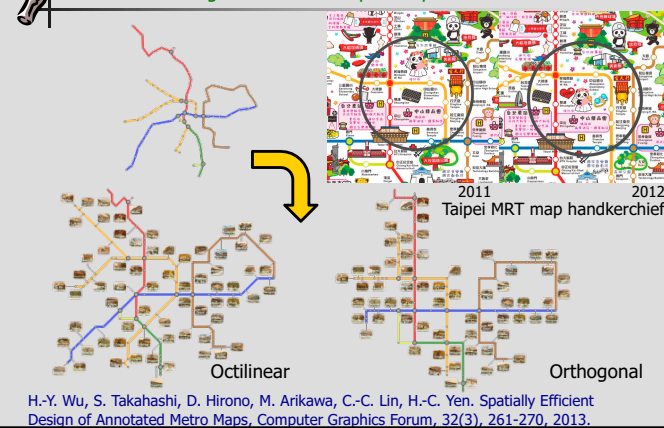


Overview



Spatially-Efficient Metro Map Layout

~Modeling Hand-Drawn Maps as Optimization Problems~





Hand-Drawn Schematic Maps



London Underground Map



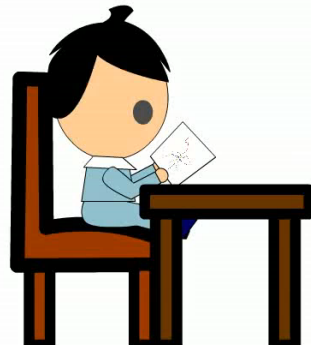
Hand-Drawn Schematic Maps



Taipei MRT map handkerchief 2012
(Courtesy of Milu Design Co., LTD, Taiwan)

EuroVis 2013, Leipzig, Germany

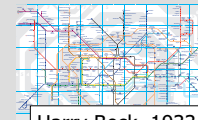
The Eurographics Conference on Visualization



Map Aesthetic Criteria

Layout

- ◆ (LH1) Edge orthogonality
- ◆ (LH2) Circular vertex order
- ◆ (LH3) Edge spacing
- ◆ (LS1) Bend minimization
- ◆ (LS2) Relative position minimization
- ◆ (LS3) Edge length minimization




Harry Beck, 1933

Map Aesthetic Criteria

Layout


- ◆ (LH1) Edge octilinearity
- ◆ (LH2) Circular vertex order
- ◆ (LH3) Edge spacing
- ◆ (LS1) Bend minimization
- ◆ (LS2) Relative position minimization
- ◆ (LS3) Edge length minimization



Harry Beck, 1933

Annotation

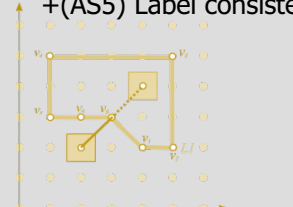
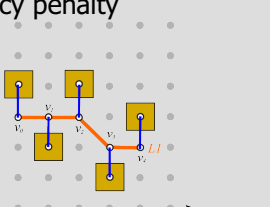
- (AH1) Leader octilinearity
- (AH2) Overlap-free layout
- (AS1) Leader orientation
- (AS2) Total leader length
- (AS3) Leader bends
- (AS4) Closed regions
- (AS5) Alternating distribution



Spatially efficient annotated map

Soft Constraints

- $C = (AS1)$ Leader orientation penalty
 + $(AS2)$ Leader length penalty
 + $(AS3)$ Leader bend penalty
 + $(AS4)$ Closed region penalty
 + $(AS5)$ Label consistency penalty

(AS4) Closed region penalty (AS5) Label consistency penalty

Label Consistency Penalty

For each enclosed region

$$\text{cost}_{(AS5)} = \sum_{f \in I_f} \text{adj}(f_j)$$

$$(f_j(v_i)) \text{XOR} (f_j(v_{i+1}))$$

$$= (f_j(v_i) \text{AND} \overline{f_j(v_{i+1})}) \text{OR} (\overline{f_j(v_i)} \text{AND} f_j(v_{i+1}))$$

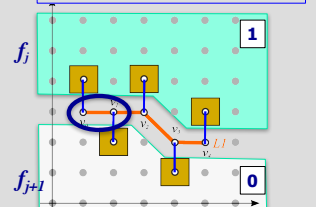
$$2a_i \leq 1 + f_j(v_i) - f_j(v_{i+1}) \leq 1 + a_i \quad \text{AND}$$

$$2b_i \leq 1 - f_j(v_i) + f_j(v_{i+1}) \leq 1 + b_i \quad \text{AND}$$

$$1 - \text{adj}_i(f_j) \leq a_i + b_i \leq 2(1 - \text{adj}_i(f_j)) \quad \text{OR}$$

AND $2x \leq x_1 + x_2 \leq 1 + x$

OR $x \leq x_1 + x_2 \leq 2x$



(AS5) Label consistency penalty

Three-Step Algorithm

Predefined layout

Overlap check

Step 1

Label Assignment

Overlap check


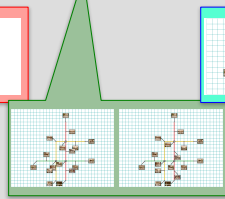

Step 2

Edge Arrangement

Overlap check

Step 3

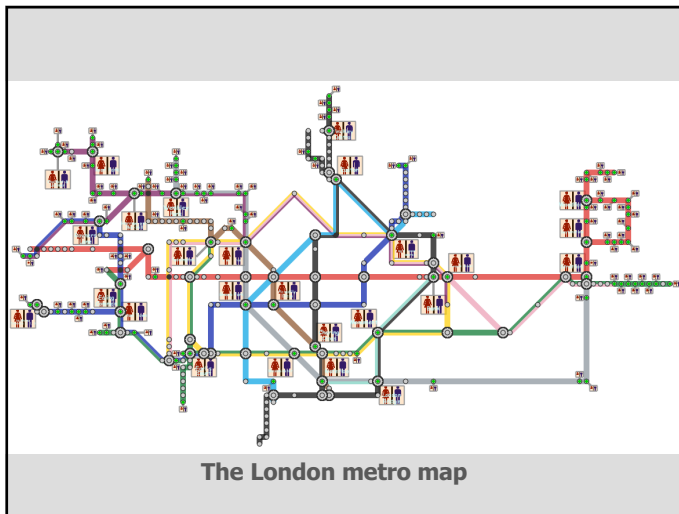
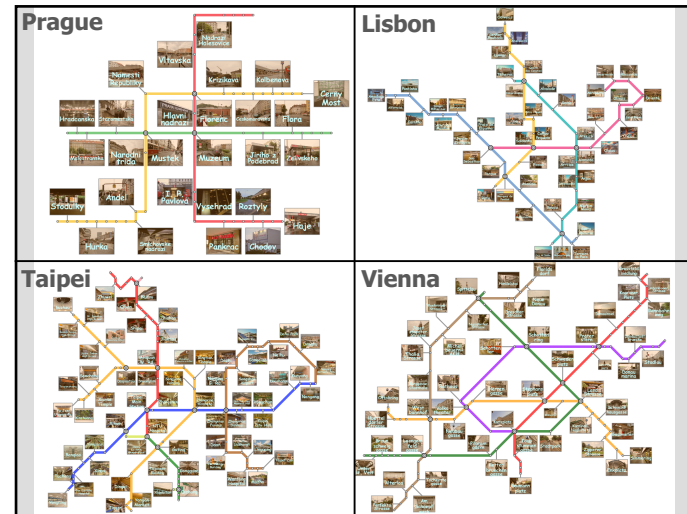
Output



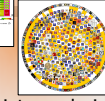
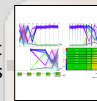
Demonstration

Design Scenario



Overview

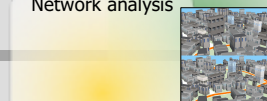
Gradient methods



Multivariate analysis

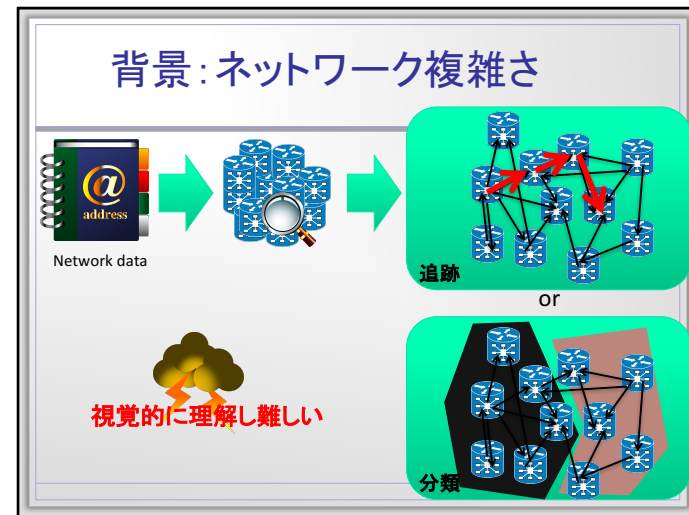
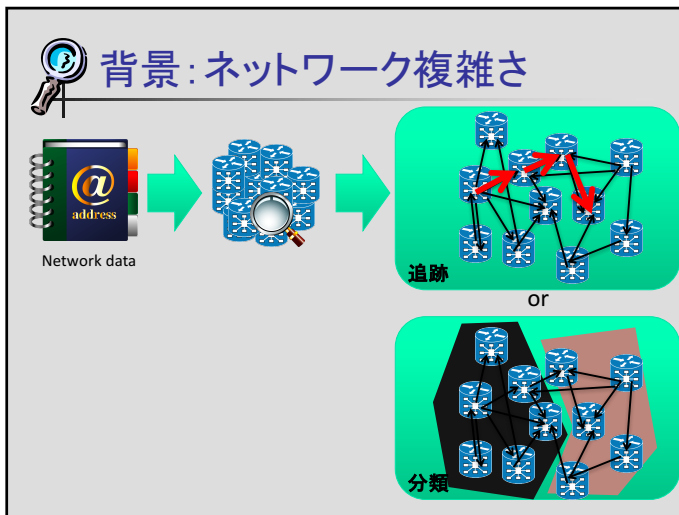
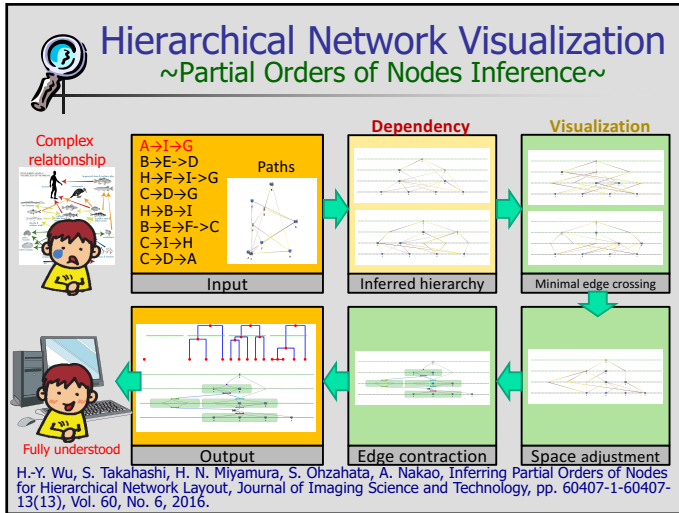
Map composition

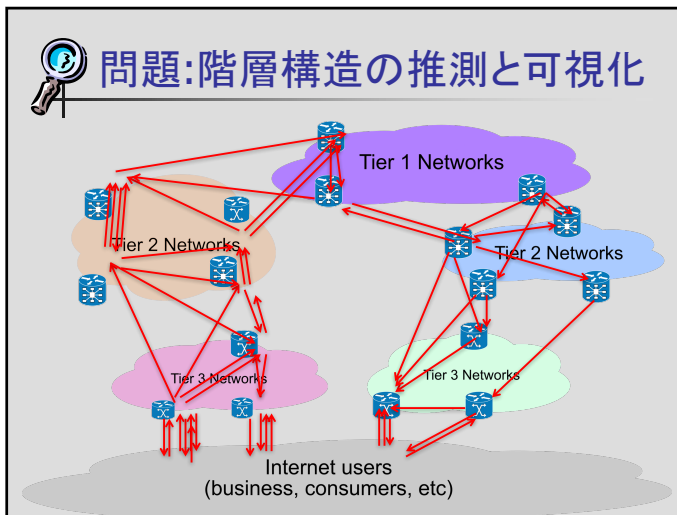
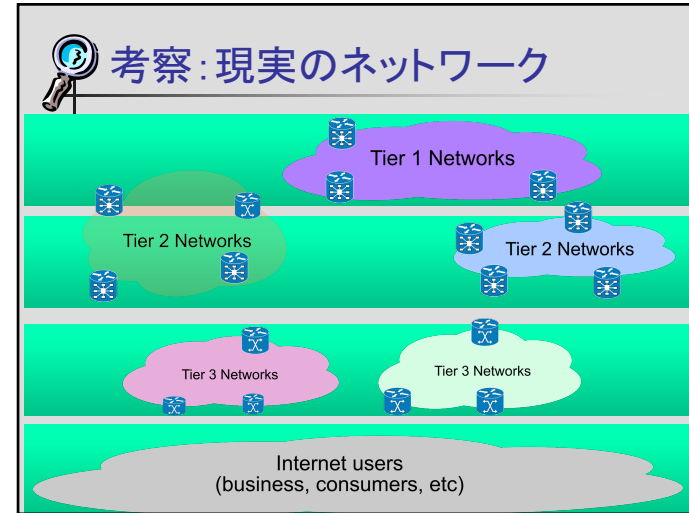
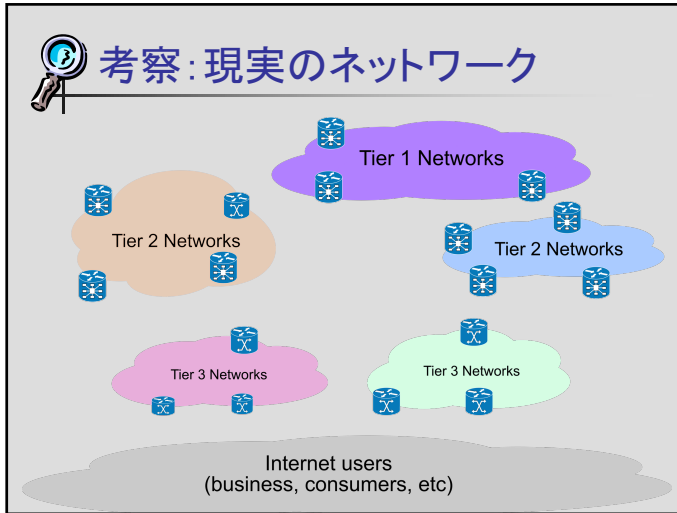
Linear programming



Integer programming







アイデア: ネットワークパスから推測

- 片道パス: パスがネットワーク階層を順々に登るものを仮定.
- 往復パス: 低階層, 高階層, 低階層と移動する山形のパスを仮定. [Gao, 2001]

片道パス

往復パス

整数計画法による最適化を用いて類推する

手法: 片道パス

$E \rightarrow G \rightarrow C \rightarrow I$
 $E \rightarrow C \rightarrow B$
 $A \rightarrow G \rightarrow H \rightarrow B$
 $A \rightarrow H \rightarrow D$
 $A \rightarrow F \rightarrow D$

入力

階層構造類推と可視化

ペナルティ, 小さければよい.

$$p(u_i) - p(u_{i+1}) \geq 1 - v_{i,i+1} \quad \text{階層ID} = 2$$

$$p(u_i) - p(u_{i+1}) \leq \lambda_{i,i+1}$$

階層ID = 3

階層IDの差, 小さければよい.

手法: 往復パス

$F \rightarrow E \rightarrow B \rightarrow H \rightarrow C \rightarrow D \rightarrow I$
 $I \rightarrow H \rightarrow C \rightarrow D \rightarrow I$
 $I \rightarrow H \rightarrow E \rightarrow A$
 $F \rightarrow E \rightarrow B \rightarrow G$

入力

階層構造類推と可視化

上りパス

$$p(u_i) - p(u_{i+1}) \geq +\alpha_{i,i+1} - M\beta_{i,i+1} - v_{i,i+1}$$

$$p(u_i) - p(u_{i+1}) \leq \lambda_{i,i+1}$$

階層ID = 2

上りパス

$$\alpha = 1, \beta = 0$$

階層ID = 3

下りパス

手法: 往復パス

上りパス

$$p(u_i) - p(u_{i+1}) \geq +\alpha_{i,i+1} - M\beta_{i,i+1} - v_{i,i+1}$$

$$p(u_i) - p(u_{i+1}) \leq \lambda_{i,i+1}$$

下りパス

$$p(u_j) - p(u_{j+1}) \leq -\beta_{j,j+1} + M\alpha_{j,j+1} + v_{j,j+1}$$

$$p(u_j) - p(u_{j+1}) \geq -\lambda_{j,j+1}$$

手法: 往復パス

上りパス

$$p(u_i) - p(u_{i+1}) \geq +\alpha_{i,i+1} - M\beta_{i,i+1} - v_{i,i+1}$$

$$p(u_i) - p(u_{i+1}) \leq \lambda_{i,i+1}$$

下りパス

$$p(u_j) - p(u_{j+1}) \leq -\beta_{j,j+1} + M\alpha_{j,j+1} + v_{j,j+1}$$

$$p(u_j) - p(u_{j+1}) \geq -\lambda_{j,j+1}$$

上りパスと下りパスは両立はしないため, 大きい整数Mを導入

$$\alpha_{j,j+1} + \beta_{j,j+1} = 1$$

手法: 往復パス ターニングポイントは1つ (山形)

階層ID= 1 $p(u_k)$

階層ID= 2 $p(u_{i+1})$ $p(u_j)$

階層ID= 3 $p(u_i)$ $p(u_{j+1})$

上りパス
 $p(u_i) - p(u_{i+1}) \geq +\alpha_{i,i+1} - M\beta_{i,i+1} - v_{i,j+1}$
 $p(u_i) - p(u_{i+1}) \leq \lambda_{i,i+1}$

下りパス
 $p(u_j) - p(u_{j+1}) \leq -\beta_{j,j+1} + M\alpha_{j,j+1} + v_{j,j+1}$
 $p(u_j) - p(u_{j+1}) \geq -\lambda_{j,j+1}$

$\alpha_{j,j+1} + \beta_{j,j+1} = 1$

$\alpha_{i,i+1} \oplus \alpha_{i+1,k} + \alpha_{i+1,k} \oplus \alpha_{k,j} \oplus \alpha_{k,j} \oplus \alpha_{j,j+1} = 1 \quad \oplus(XOR)$

手法: 往復パス ターニングポイントは1つ (山形)

階層ID= 1 $p(u_k)$

階層ID= 2 $p(u_{i+1})$ $p(u_j)$

階層ID= 3 $p(u_i)$ $p(u_{j+1})$

上りパス
 $p(u_i) - p(u_{i+1}) \geq +\alpha_{i,i+1} - M\beta_{i,i+1} - v_{i,j+1}$
 $p(u_i) - p(u_{i+1}) \leq \lambda_{i,i+1}$

下りパス
 $p(u_j) - p(u_{j+1}) \leq -\beta_{j,j+1} + M\alpha_{j,j+1} + v_{j,j+1}$
 $p(u_j) - p(u_{j+1}) \geq -\lambda_{j,j+1}$

$\alpha_{j,j+1} + \beta_{j,j+1} = 1$

最小化 $\text{minimize } w_1 \times \lambda_{i,i+1} + w_2 \times v_{i,i+1}$

$\alpha_{i,i+1} \oplus \alpha_{i+1,k} + \alpha_{i+1,k} \oplus \alpha_{k,j} \oplus \alpha_{k,j} \oplus \alpha_{j,j+1} = 1 \quad \oplus(XOR)$

A Short Demonstration

User Intervention

Applications 1: One-way Path

- Curricula of Univ. of Aizu

Force-directed layout Hierarchical layout

Reverse paths are more penalized Numbers of credits are equalized at the respective layers

Applications 2: Round-trip Path

- Tokyo metro
 - 255 stations
 - 13 metro lines

Accessibility zones inferred from the metro network

Visualizing hierarchies among the metro stations

Applications 3: Round-trip Path

- P2P network
 - 116 nodes, 306 edges, and 525 paths

Hierarchical structures Grouped nodes Edge contraction

Optimized layout large-sized P2P network

Overview

Gradient methods

Genetic algorithms

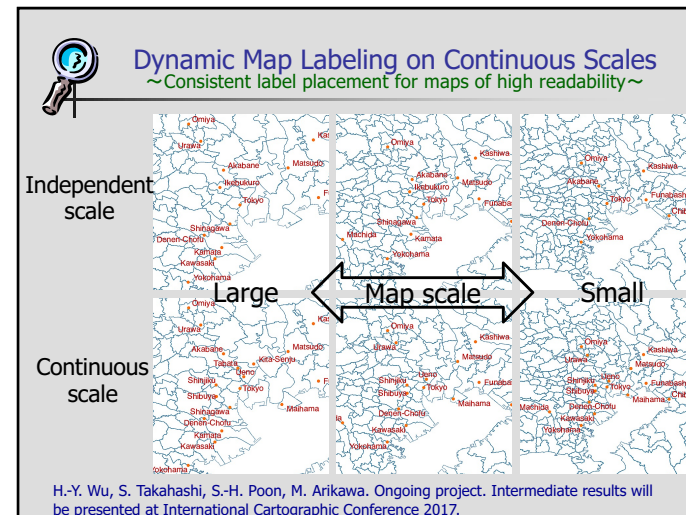
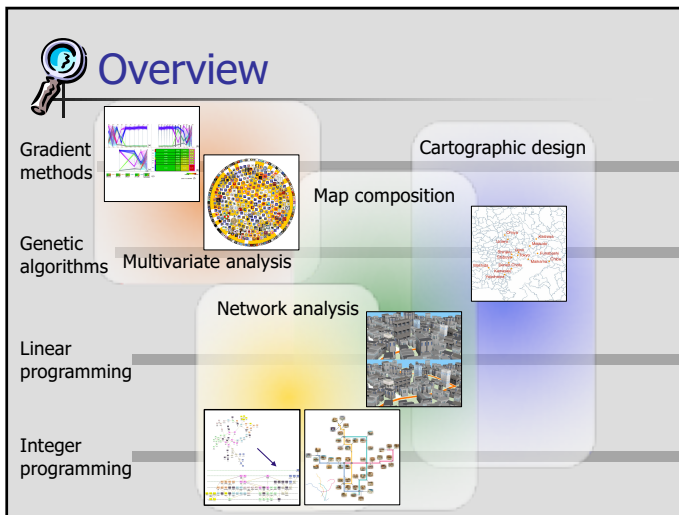
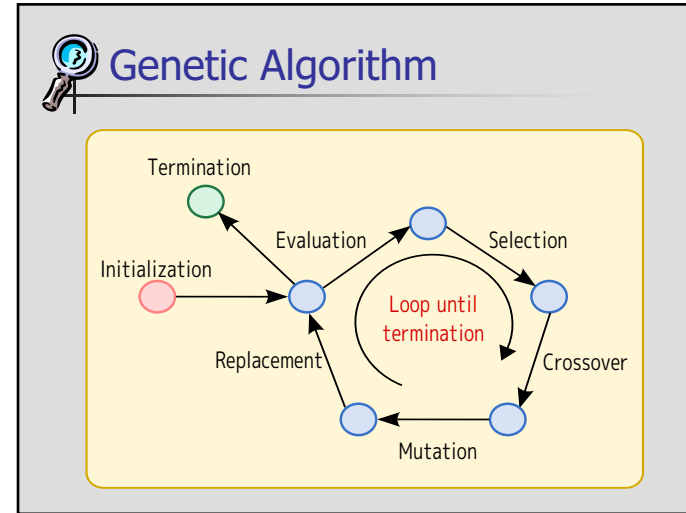
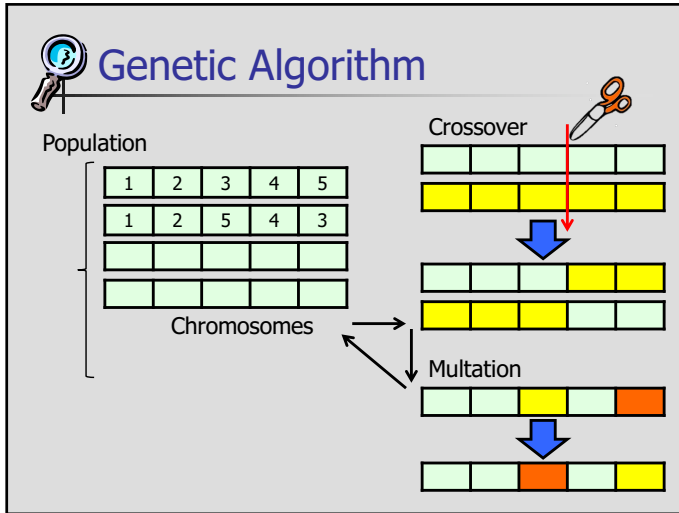
Linear programming

Integer programming

Map composition

Multivariate analysis

Network analysis





デジタルマップの普及

- 異なるスケール(縮尺)による地図表示



109



ラベル配置の問題点

- スケールの変化にラベル出現消滅する



110



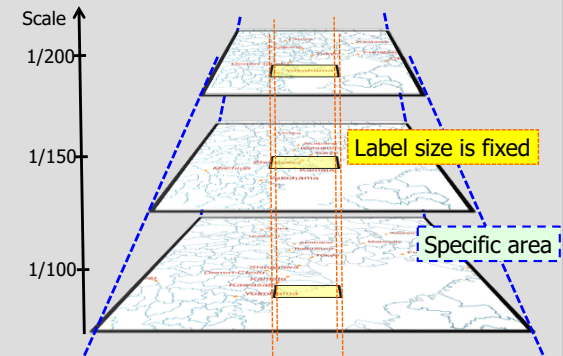
Objectives

- Optimize label placement on the map
- Retain the consistency in labeling over the map scale



Scale-Aware Label Placement

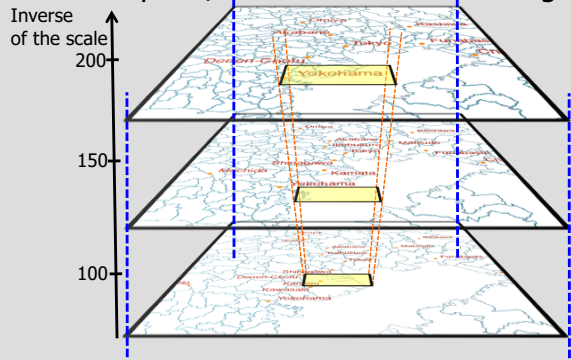
- Specific area shrinks as the scale reduces





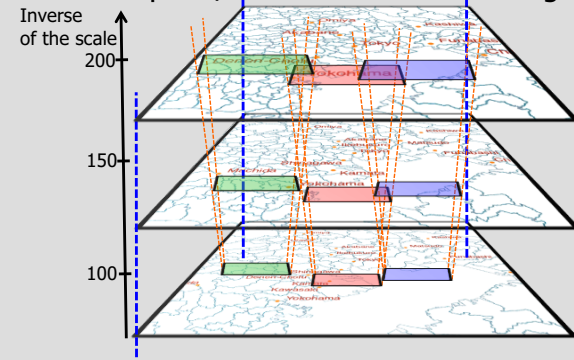
Scale-Aware Label Placement

- Labels expand/shrink as the scale changes



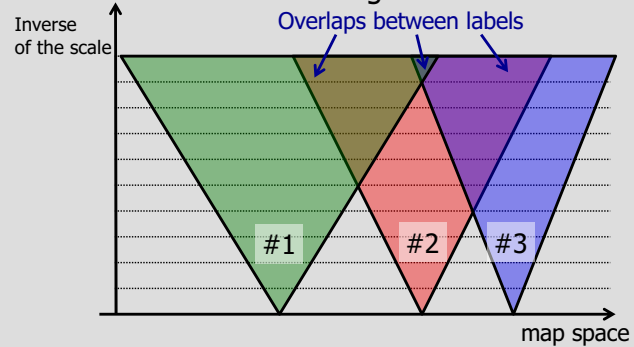
Scale-Aware Label Placement

- Labels expand/shrink as the scale changes



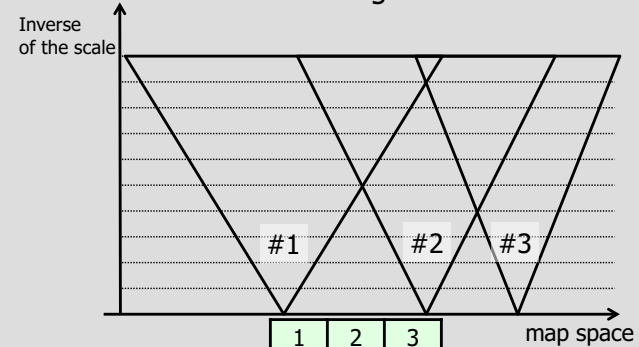
Scale-Aware Label Placement

- Select labels according to the scale



Scale-Aware Label Placement

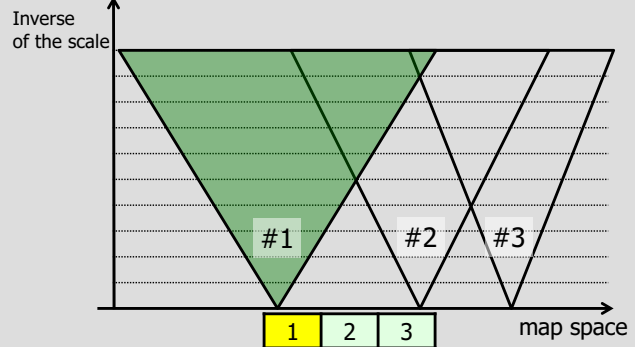
- Select labels according to the scale





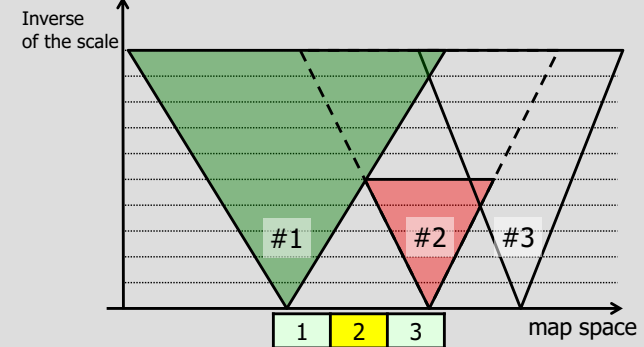
Scale-Aware Label Placement

- Select labels according to the scale



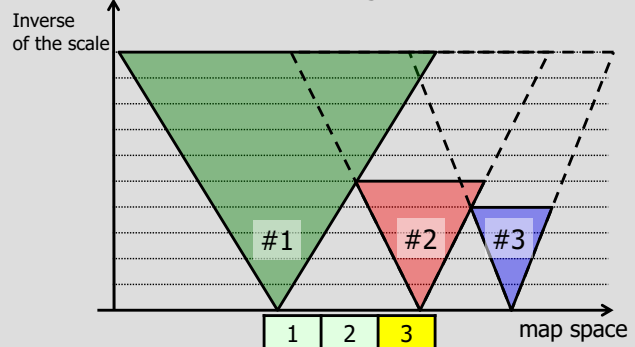
Scale-Aware Label Placement

- Select labels according to the scale



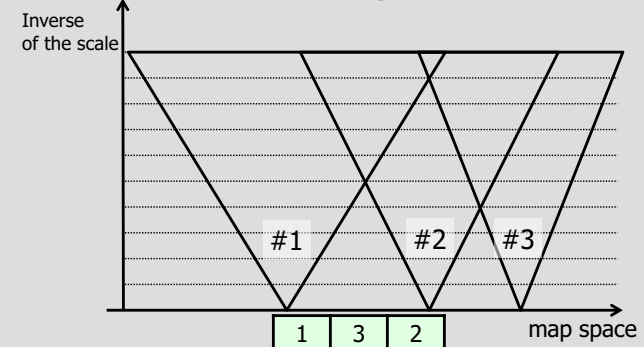
Scale-Aware Label Placement

- Select labels according to the scale



Scale-Aware Label Placement

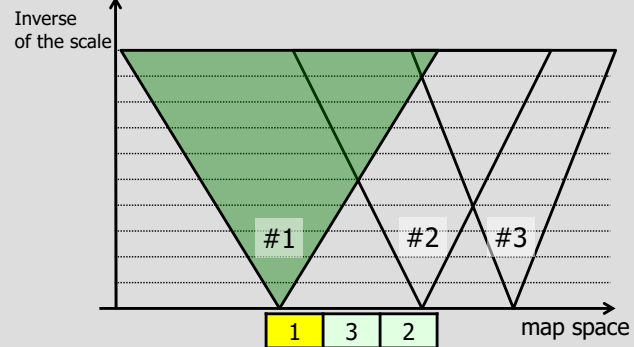
- Select labels according to the scale





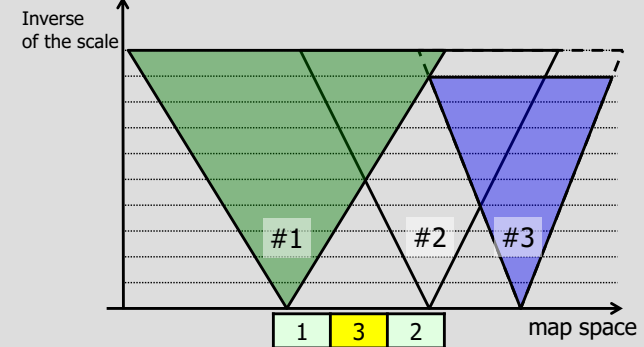
Scale-Aware Label Placement

- Select labels according to the scale



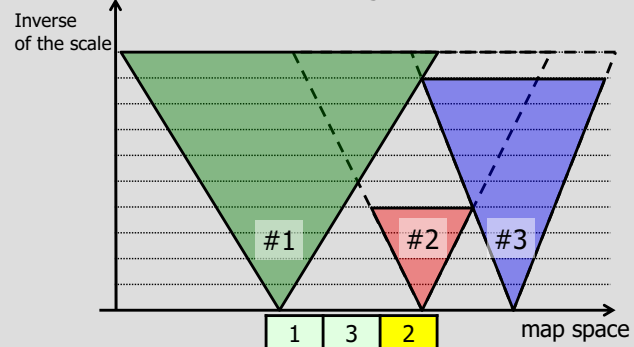
Scale-Aware Label Placement

- Select labels according to the scale



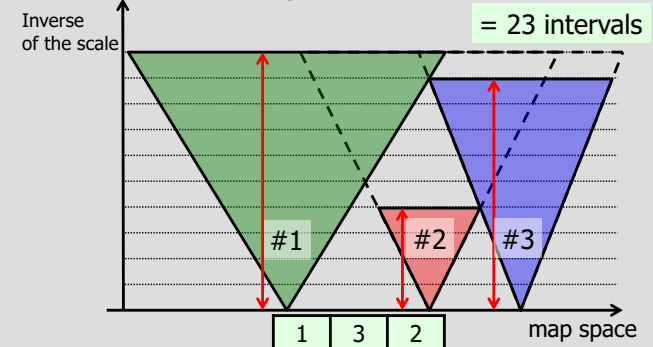
Scale-Aware Label Placement

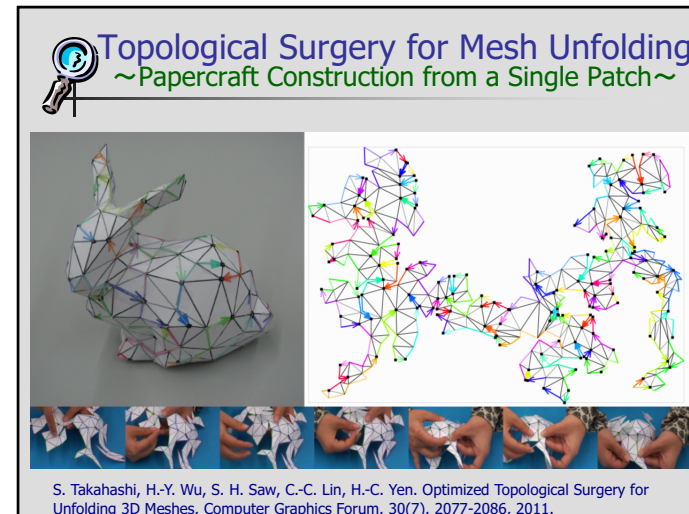
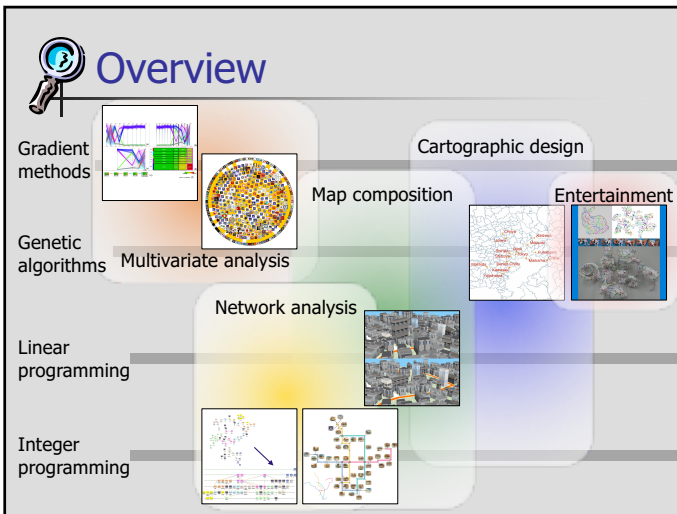
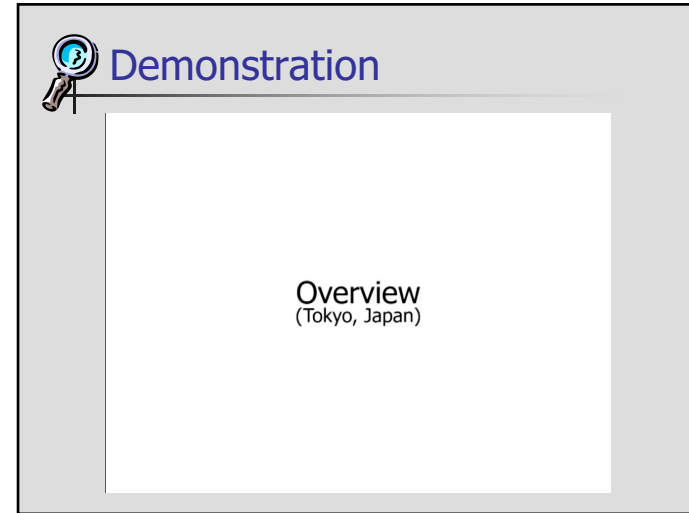
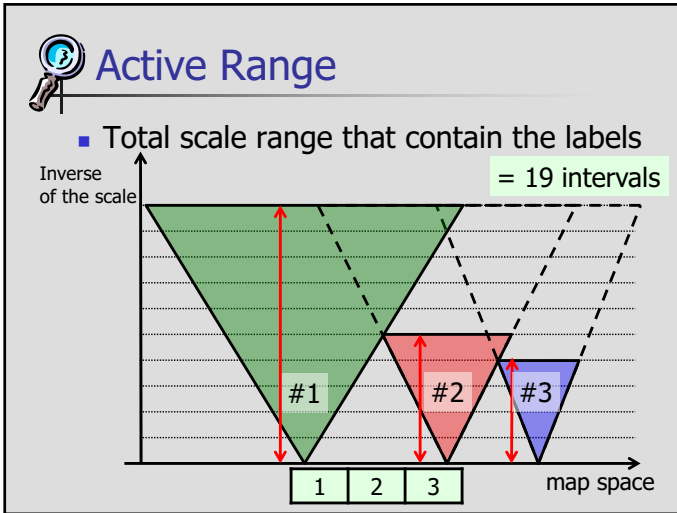
- Select labels according to the scale



Active Range

- Total scale range that contain the labels

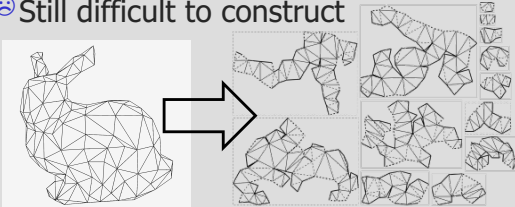






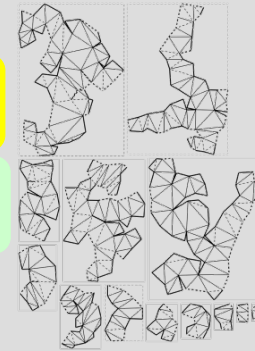
Papercraft Models

- ☺ Can retrieve 3D physical shapes
- ☺ For preparing the miniatures of 3D scenes
- ☺ Fun for both children and adults
- ☹ Still difficult to construct



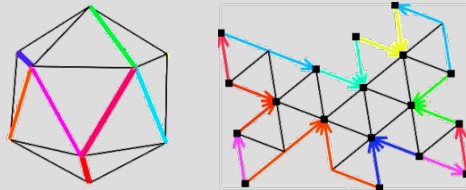
Why Difficult?

- Practical issues
 - Large number of unfolded patches, including small fragments
 - Troubles in finding correspondence between a pair of cut edges



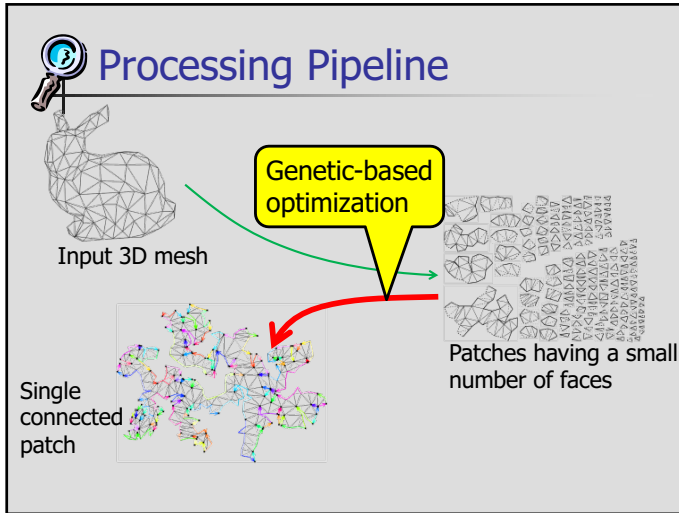
Key Ideas

- Employ the topological surgery to encode the boundary edges of the unfolded patch
- Genetic-based approach to unfolding a 3D mesh into a single connected patch



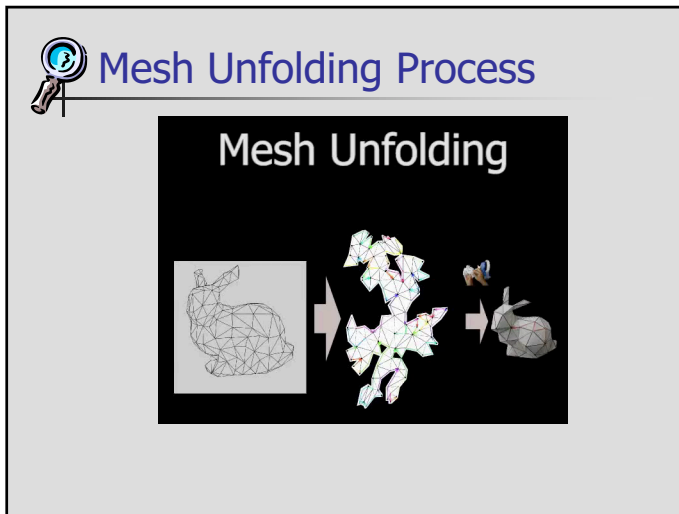
Papercraft Construction Example

Papercraft Construction Example



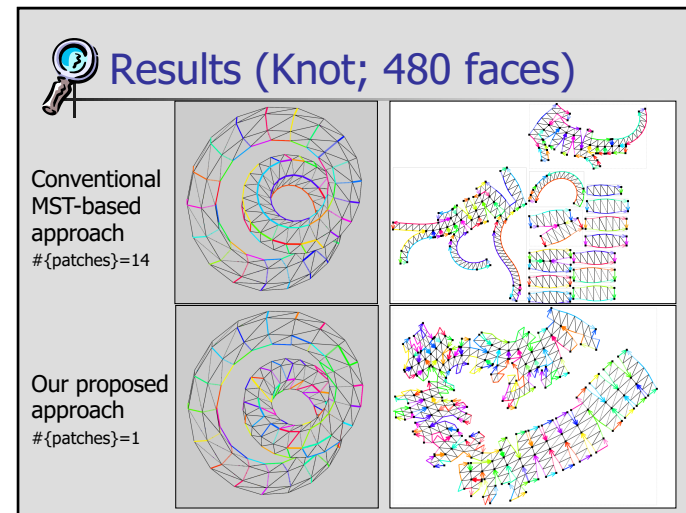
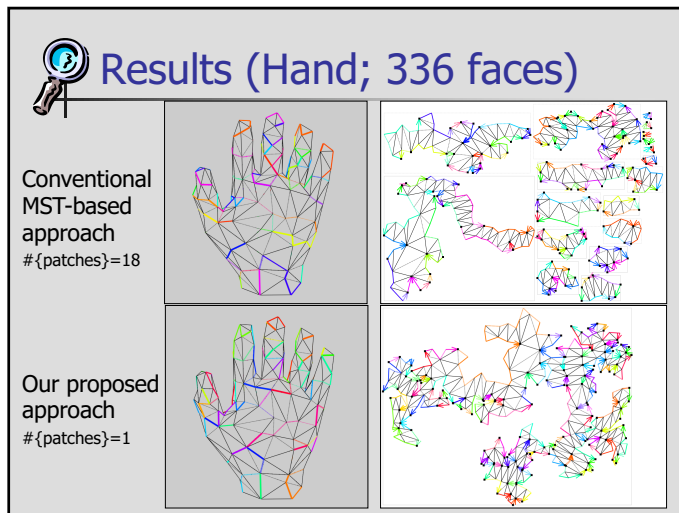
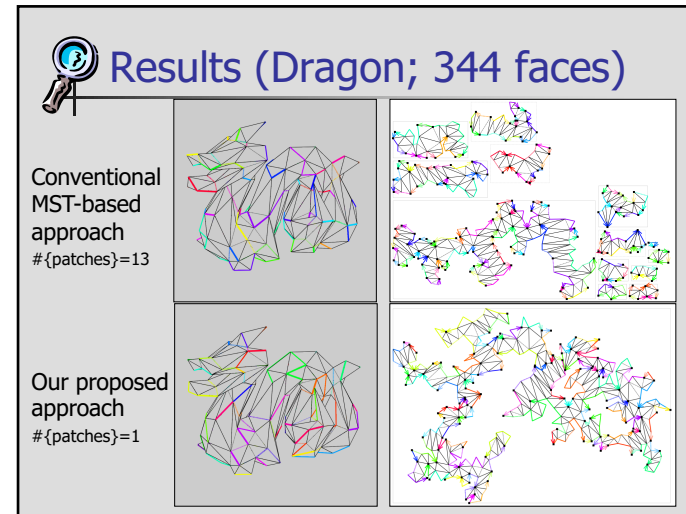
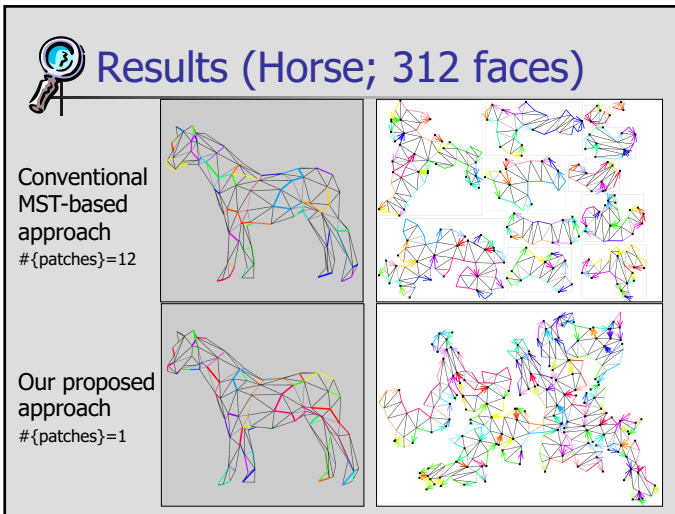
Stitching Unfolded Patches

- Encode the order of edges to be stitched together as a chromosome
- Apply a genetic algorithm with improved crossover and mutation operations



Results (Bunny; 348 faces)

Conventional MST-based approach #{patches}=13		
Our proposed approach #{patches}=1		



Results (Cat; 702 faces)

<p>Conventional MST-based approach #{patches}=28</p>		
<p>Our proposed approach #{patches}=1</p>		

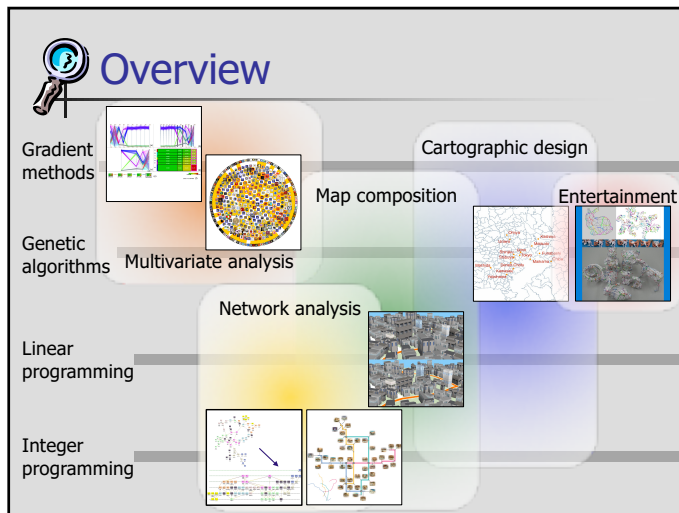
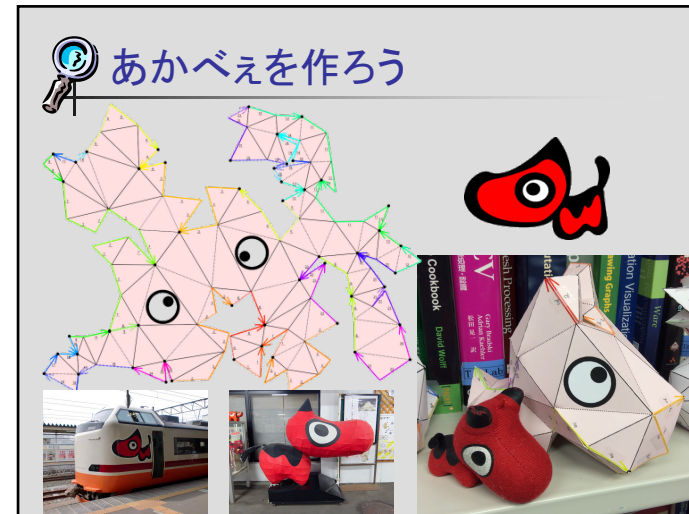
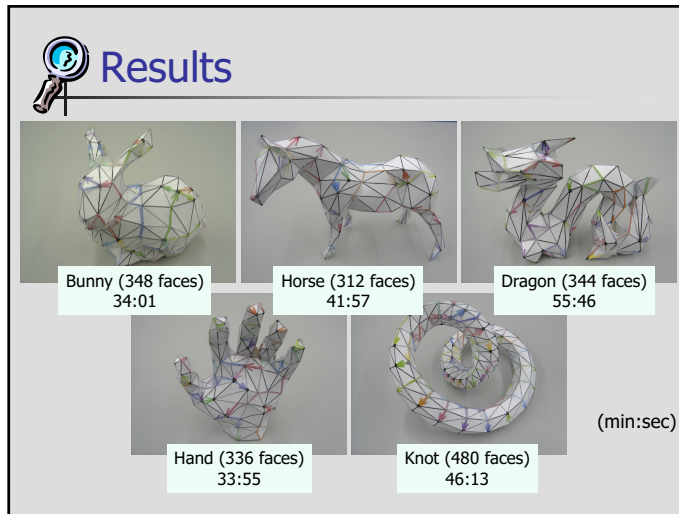
Results (Fish; 950 faces)

<p>Conventional MST-based approach #{patches}=31</p>		
<p>Our proposed approach #{patches}=1</p>		

Papercraft Construction

Let's Try!

Papercraft Construction



- ## おわりに
- 情報可視化における幅広い技術課題を統一的に最適化問題として定式化
 - 多変量データ視覚解析
 - ネットワークデータ可視化
 - 地図の図式表現と設計
 - おまけ: 娯楽
 - 個々の問題をどのようにモデル化するか
が解決への糸口に



おわり